## Understanding the Gender Division of Work across Countries

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Gender-Sensitive Economic Recovery and Resilience in Asia Conference Tokyo, 9 March 2023

## This paper

- 1. How does work differ across countries?
- → New facts on gender division of market and non-market work.
- 2. Accounting framework
- ightarrow Income effects, spousal income, norms, discrimination, labor productivity ...
- 3. Study drivers of changes in hours worked
- → Cross-country and country studies (USA, TZA, IND, FRA)

### 1. How does work differ across countries?

#### Market work

- Higher in poor countries (Bick, Fuchs-Schündeln and Lagakos 2018).
- More female market work in HIC
- Less male market work in HIC (Aguiar et al. 2021)

#### Non-market work

- More home production in poor countries (Bridgman et al. 2018).

### Know less about

- Types of non-market work: <u>care</u> and <u>domestic</u> work  $\rightarrow$  Total work.
- Gender division
- Whole country income distribution.
- $\rightarrow$  We fill these gaps thanks to an extensive data harmonization exercise.

## 2. What determines choices of work and its gender division?

- Culture: Fernandez, Fogli and Olivetti (2004) and Fernandez (2013)
- Bargaining power: marriage laws Chiappori, Fortin and Lacroix (2002) & Greewood, Guner, Kocharkov & Santos (2016).
- Parenting style: Doepke and Zilibotti (2019)
- Income: labor market discrimination & occupational preferences Hsieh, Hurst, Jones and Klenow (2019), Chiplunkar and Kleineberg (2022)
- Marketization of services: Ngai & Petrongolo (2017)
- Home production: technology Greenwood, Seshadri and Yorukoglu (2005)
- → "Little to no work explores the ability of such models to account for heterogeneity in women's rights in the entire cross-section of countries." Tertilt, Doepke, Hannusch and Montenbruck (2022)

## 3. Accounting framework and decomposition exercise.

- Model of household allocation of work.
  - Framework that accounts for a rich set of channels.
  - Wages (own + spouse), disutilities of work, productivity of non-market work and bargaining.
- Direct and transparent identification of each parameter.
  - By gender and marital status.
  - Calibration to 30 countries.

- Use model as an accounting framework

# Data

### Data

We leverage two micro datasets that we built:

1. Harmonized World Time Use Survey (HWTUS)

2. Harmonized World Labour Force Survey (HWLFS)

## Data: Harmonized World Time Use Survey (HWTUS)

#### Individual level information

- household roster
- demographic
- education
- 24 hour diary data.

#### Coverage

- 137 surveys from 42 countries.
- \$1,500 (TZA 2006) \$100,000 (LUX 2015)

#### Data sources

- MTUS and CTUR.
- Time use surveys and household surveys from NSO.

## Data: Harmonized World Labour Force Survey (HWLFS)

#### Individual level information

- household roster
- demographic
- education
- employment status, jobs and wages

### Coverage:

- 1'748 country-year surveys
- 105 countries
- \$302 (SOM 2016) \$115,000 (LUX 2020)

#### Data sources:

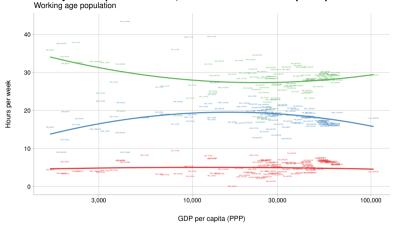
- Nests traditional data sources (IPUMS Intl., IPUMS-US historical and EU-LFS).
- Household and labour force surveys from NSO and World Bank

## Data: Measurement

Activity	Type of work	Definition	ICATUS	SNA
Work		Activities that can be delegated to a third party		
	Market	<ul><li>Production of goods and services destined to the market</li><li>Production of goods for own final use.</li></ul>	1 2	Y Y
		Activities to produce services for own final use:		
	Services Care	<ul><li>Domestic services</li><li>Household and family members.</li><li>Others (incl. volunteering and community work).</li></ul>	3 4 5	N N N
Education		Education and related activities.	6	
Leisure		Socializing, community participation and religious practice. Culture, leisure, mass-media and sports practices	7 8	
Self-care		Activities for self-care and maintenance (sleep, food, cleaning).	9	

Table: ICATUS activity classification - 1 digit.

### Weekly hours spent on market, domestic and care work per capita

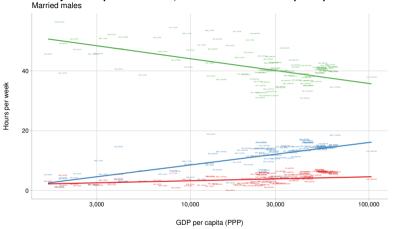


Hours on: - domestic care - domestic services - market work

Quadratic fit, shaded area marks the 95% confidence interval
Working age population. Activity groups are aggregated based on the ICATUS 2016 one-digit codes [market = 18.2, services = 3, care = 485]. Minimum sample size for each activity group is 30.



#### Weekly hours spent on market, domestic and care work per capita

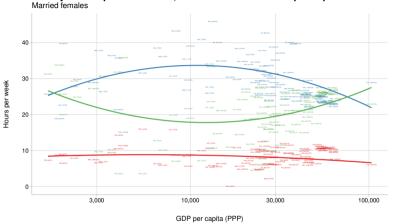


Hours on: - domestic care - domestic services - market work

Male, married working age population. Activity groups are aggregated based on the ICATUS 2016 one-digit codes [market = 18.2, services = 3, care = 48.5]. Minimum sample size for each activity group is 30.



#### Weekly hours spent on market, domestic and care work per capita

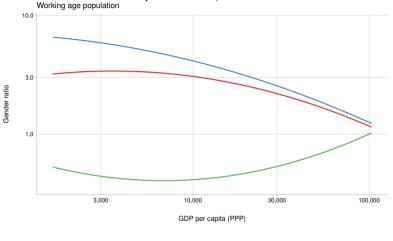


Hours on: - domestic care - domestic services - market work

Quadratic fit, shaded area marks the 95% confidence interval
Female, married working age population. Activity groups are aggregated based on the ICATUS 2016 one-digit codes [market = 182, services = 3, care = 485]. Minimum sample size for each activity group is 30.



#### Gender ratio of hours spent on market, domestic and care work



Work type: - domestic care - domestic services - market work

Quadratic fit, shaded area marks the 95% confidence interval

Working age population. Activity groups are aggregated based on the ICATUS 2016 one-digit codes [market = 18.2, services = 3, care = 485]. Minimum sample size for each activity group is 30.



## Facts on work across countries: Summary

Fact 1: U-shape pattern of women market work with country income level.

Fact 2: Hump shape of women domestic work with country income level.

Fact 3: Men in rich countries do less market than in poor countries.

Fact 4: Men in rich countries do more care and service work than in poor countries.

What determines these patterns?

# Model

## Model: Markets, Technology and Budget Constraints

- Two types of households: married and single.
- Three goods: market good  $(c_m)$ , domestic good/service  $(c_d)$  and care services  $(c_c)$
- Three activities: market  $(L_m)$ , domestic  $(L_d)$  and care  $(L_c)$
- Home technology:  $y_i = z_i L_i$ , where i = c, d.

## Model: Preferences and budget constraints

Individual preferences:

$$u = \frac{C^{1-\sigma}}{1-\sigma} - D_m \frac{L_m^{1+\frac{1}{\phi}}}{1+\frac{1}{\phi}} - D_d \frac{L_d^{1+\frac{1}{\phi}}}{1+\frac{1}{\phi}} - D_c \frac{L_c^{1+\frac{1}{\phi}}}{1+\frac{1}{\phi}}.$$

$$C = \left[ c_m^{\frac{\varepsilon - 1}{\varepsilon}} + B_d c_d^{\frac{\varepsilon - 1}{\varepsilon}} + B_c c_c^{\frac{\varepsilon - 1}{\varepsilon}} \right]^{\frac{\varepsilon}{\varepsilon - 1}}$$

Utility of couples:

$$U = \lambda u^m + (1 - \lambda)u^f$$

Budget constraints of couples:

$$P(c_{m}^{m} + c_{m}^{f}) = w^{m} L_{m}^{m} + w^{f} L_{m}^{f}$$
$$c_{i}^{m} + c_{i}^{f} = z_{i} (L_{i}^{f} + L_{i}^{m}) \quad i = \{c, d\}$$



### Model: Allocation

#### Derived individual utility:

$$u^{g} = \frac{1}{1 - \sigma} \left[ c_{m}^{\frac{\varepsilon - 1}{\varepsilon}} + B_{d} \left( z_{d} L_{d}^{g} \right)^{\frac{\varepsilon - 1}{\varepsilon}} + B_{c} \left( z_{c} L_{c}^{g} \right)^{\frac{\varepsilon - 1}{\varepsilon}} \right]^{\frac{\varepsilon (1 - \sigma)}{\varepsilon - 1}} - D_{m} \frac{L_{m}^{1 + \frac{1}{\phi}}}{1 + \frac{1}{\phi}} - D_{d} \frac{L_{d}^{1 + \frac{1}{\phi}}}{1 + \frac{1}{\phi}} - D_{c} \frac{L_{c}^{1 + \frac{1}{\phi}}}{1 + \frac{1}{\phi}}.$$

- Production efficiency:  $\omega_i = B_i z_i^{1-\frac{1}{\varepsilon}}$  where  $i = \{c, d\}$
- Separating  $z_i$  from  $B_i$  is not feasible without observing  $c_i$ .
- Equilibrium allocation depends only on  $\omega_i$ .

▶ FOCs

### Model: Allocation: Within household division of work

#### Care/Domestic hours, men vs women

$$\frac{L_i^f}{L_i^m} = \left(\frac{D_i^m}{D_i^f} \frac{\lambda}{1 - \lambda}\right)^{\phi}$$

#### Market hours, men vs women

$$\frac{L_m^f}{L_m^m} = \left(\frac{w^f}{w^m} \frac{D_m^m}{D_m^f} \frac{\lambda}{1 - \lambda}\right)^{\phi}$$



## Model: Allocation: Time spent across work types

#### Care hours vs Market hours, men vs women

$$\left(\frac{L_m^m}{L_c^m}\right)^{\frac{1}{\phi}} = \left(\frac{L_m^f}{L_c^f}\right)^{-\frac{1}{\varepsilon}} \frac{1}{\omega_c} \frac{D_c^m}{D_m^m} \left(\frac{1}{P} \frac{w^m \Delta_m + w^f}{\Delta_c + 1}\right)^{-\frac{1}{\varepsilon}} \frac{w^m}{P}$$

#### Domestic hours vs Market hours, men vs women

$$\left(\frac{L_m^m}{L_d^m}\right)^{\frac{1}{\phi}} = \left(\frac{L_m^f}{L_d^f}\right)^{-\frac{1}{\varepsilon}} \frac{1}{\omega_d} \frac{D_d^m}{D_m^m} \left(\frac{1}{P} \frac{w^m \Delta_m + w^f}{\Delta_d + 1}\right)^{-\frac{1}{\varepsilon}} \frac{w^m}{P}$$



### Model: Allocation: Levels

#### Market hours worked

$$L_{m}^{f \sigma + \frac{1}{\phi}} = \frac{1}{D_{m}^{f}} (1 - \Lambda)^{-\sigma} (\Omega(\omega_{c}; \omega_{d}) \Theta_{c}^{f})^{\frac{1 - \sigma \varepsilon}{\varepsilon}} \left( \frac{w^{m} \Delta_{m} + w^{f}}{P} \right)^{-\frac{1}{\varepsilon}} \frac{w^{f}}{P}.$$

$$L_{m}^{m\sigma + \frac{1}{\phi}} = \frac{1}{D_{m}^{m}} \left( \frac{\Lambda}{\Delta_{m}} \right)^{-\sigma} (\Omega(\omega_{c}; \omega_{d}) \Theta_{c}^{f})^{\frac{1 - \sigma \varepsilon}{\varepsilon}} \left( \frac{w^{m} \Delta_{m} + w^{f}}{P} \right)^{-\frac{1}{\varepsilon}} \frac{w^{m}}{P}.$$

where  $\Delta_i$  are gender ratios of time worked in activity i.

#### **Determinants:**

- Own + spousal wage
- Disutility of market work
- Consumption level  $\Omega(\omega_c, \omega_d)$
- Share of consumption  $(1 \Lambda)$



# Calibration

### Calibration:

- Data
  - Use HWLFS to measure  $L_m^g$ ,  $w^g$
  - Use HWTUS to measure  $L_d^g$ ,  $L_c^g$
- Model
  - 9 parameters  $(\omega_c, \omega_d, D_m^g, D_d^g, D_c^g, \lambda)$
  - Allocation consists of 6 equations.
- Impose structure on D.
- Ass 1: Common disutility of care work  $(D_c^f = D_c^m)$
- Ass 2: Assume  $D_c^m = D^m$
- Ass 3: Assume  $\frac{D_d^f + D_d^m}{2} = D^m$ 
  - ▶ Step 1
     ▶ Step 2
     ▶ Step 3
     ▶ Step 4

### Calibration:

- Set parameters  $\varepsilon=2$  as in Aguiar, Hurst and Karabarbounis (2012)
- External calibration of elasticity  $(\sigma, \phi)$ .
  - Choose  $\sigma$  such that  $D^m$  is constant in the US time series (1975-2018).
  - We get  $\sigma$ =1.28,  $\phi$ =0.6.
  - In line with Blundell, Pistaferri and Saporta-Eksten (2016).
- Internal calibration parameters

  - 2. US time series (1975-2013) (1975-2013)

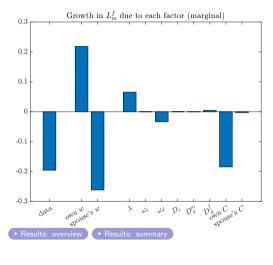
# Results

### Results

- Fact 1: U-shape pattern of women market work with country income level.
  - 1. Drop in women market hours  $L_m^f$
  - 2. Increase in women market hours  $L_m^f$
- Fact 2: Hump shape of women domestic work with country income level.
  - 1. Increase in women domestic hours  $L_d^f$
  - 2. Decrease in women domestic hours  $L_d^f$
- Fact 3: Men in rich countries do less market work than in poor countries.
- Fact 4: Men in rich countries do more care and service work than in poor countries.

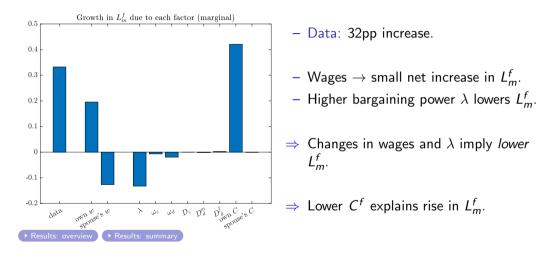
▶ Results: summary

# Understanding fact 1.1 : $\downarrow$ Market hours of married female $L_m^f$

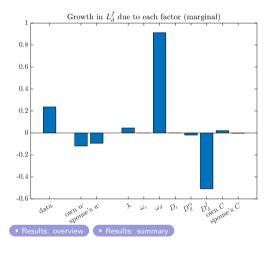


- Data: 20 pp drop
- Own wage : IE < SE
- Offset by income effect from spousal wage.
- Disutility of market work.

# Understanding fact 1.2 : $\uparrow$ Market hours of married female $L_m^f$

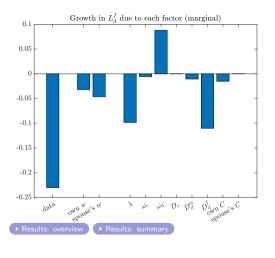


# Understanding fact 2.1 : $\uparrow$ Domestic hours of married female $L_d^f$



- Data: 22 pp increase
- Higher female wages reduce female domestic hours by 12%
- Higher productive efficiency of domestic services  $(\omega_d)$
- Greater disutility of female domestic work  $(D_d^f)$

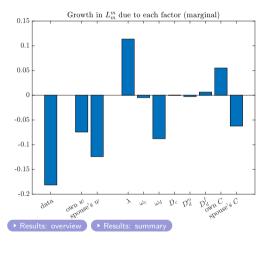
# Understanding fact 2.2 : $\downarrow$ Domestic hours of married female $L_d^f$



Data: 23pp drop.

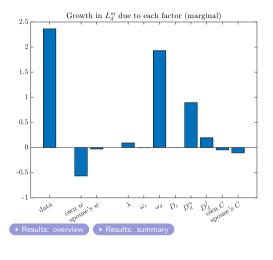
- Higher bargaining power  $(\lambda)$
- Decrease in rel. disutility of domestic work  $D_d^f$
- Offset by increase productive efficiency of domestic work  $(\omega_d)$

# Understanding fact 3: $\downarrow$ Market hours of married males $L_m^m$



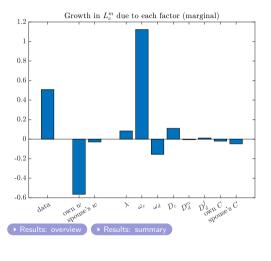
- Data: 18pp drop.
- Own wage (IE>SE)
- Offsetting effect due to loss in bargaining power  $(\lambda)$
- Increase in productivity of domestic services  $(\omega_d)$  enhances reallocation of time away from market.

# Understanding fact 4.1: $\uparrow$ Domestic hours of married males $L_d^m$



- Data: 250pp increase.
- Increase in productive efficiency of domestic work  $(\omega_d)$ .
- Lower disutility of domestic work for men.
- Contribution of higher wage.

# Understanding fact 4.2 : $\uparrow$ Care hours of married males $L_c^m$



- Data: 50pp increase
- Household productivity for care work.
- Change in wages

## Results: Summary

- Fact 1: U-shape pattern of women market work with country income level.
  - 1. Drop in women market hours  $L_m^f \leftarrow$ Spousal wage
  - 2. Increase in women market hours  $L_m^f \leftarrow \textbf{Disutility of women market work}$
- Fact 2: Hump-shape pattern of women domestic work with country income level.
  - 1. Increase in women domestic hours  $L_d^f \leftarrow \mathbf{Productivity}$  of domestic services
  - 2. Decrease in women domestic hours  $\check{L}_d^f \leftarrow \mathbf{Bargaining}$  power
- Fact 3: Men in rich countries do less market work than in poor countries.
  - 1. Decrease in male market hours  $L_m^m \leftarrow$  Income effects (own + spouse).
- Fact 4: Men in rich countries do more domestic and care work than in poor countries.
  - 1. Increase in male domestic hours  $L_d^m \leftarrow \textbf{Productivity of domestic work}$
  - 2. Increase in male care hours  $L_c^m \leftarrow \mathbf{Productivity}$  of care work

### Conclusion

- New facts on gender division of work across countries
- Develop of model of household labor supply
- Use model to disentangle channels that drive these patterns.
- Future work:
  - Correlate estimated parameters with value surveys/religion/laws.
  - Country experiences (TZA, IND, KHM, PSE, FRA)

# **Appendix**

### US parameter estimates: utility weights

#### Care hours, male vs female:

$$\left(\frac{L_c^f}{L_c^m}\right)^{\frac{1}{\phi}} = \frac{\lambda}{1-\lambda}$$

$$\frac{1975}{L_c^f/L_c^m} = \frac{2}{1.76} = \frac{1.66}{1.56}$$

$$\frac{1.56}{\lambda} = \frac{1.76}{0.85} = \frac{1.76}{0.85} = \frac{1.76}{0.85} = \frac{1.76}{0.75}$$



## US parameter estimates: relative disutility of domestic services

#### Domestic service hours, male vs female:

$$\left(\frac{L_d^f}{L_d^m}\right)^{\frac{1}{\phi}} = \frac{D_d^m}{D_d^f} \frac{\lambda}{(1-\lambda)}$$

	1975	2003	2008	2013
$L_c^f/L_c^m$	2	1.76	1.66	1.56
$\lambda$	0.85	0.80	0.78	0.75
$\frac{L_d^f/L_d^m}{D_d^f/D_d^m}$	2.54	1.58	1.57	1.54
$D_d^f/D_d^m$	0.55	1.29	1.15	1.04

▶ Back

## US parameter estimates: relative disutility of market work

Market hours, male vs female:

$$\frac{C^f}{C^m} = \frac{\lambda}{1 - \lambda} \left(\frac{L_m^m}{L_m^f}\right)^{\frac{1}{\phi}} \frac{w^f h^f}{w^m h^m}$$

$$\frac{1975}{\lambda} = \frac{2003}{0.85} = \frac{2008}{0.78} = \frac{2013}{0.75}$$

$$\frac{L_c^f/L_c^m}{\lambda} = \frac{2}{0.85} = \frac{1.76}{0.80} = \frac{1.66}{0.78} = \frac{1.56}{0.75}$$

$$\frac{L_d^f/L_d^m}{D_d^f/D_d^m} = \frac{2.54}{0.55} = \frac{1.58}{1.29} = \frac{1.57}{1.15} = \frac{1.54}{1.04}$$

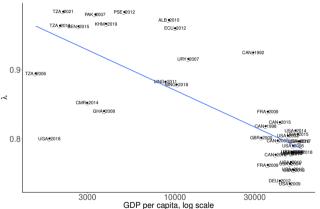
$$\frac{w_m^f/w_m^m}{w_m^f/w_m^m} = \frac{0.54}{0.64} = \frac{0.64}{0.65} = \frac{0.68}{0.66}$$

$$\frac{L_m^f/L_m^m}{C^f/C^m} = \frac{0.46}{0.92} = \frac{0.63}{0.828} = \frac{0.79}{0.79} = \frac{0.93}{0.93}$$



### Cross-country parameter estimates: Utility weight $\lambda$



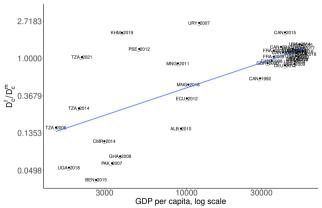


Drop in  $\frac{L_c^f}{L_c^m}$  across countries  $\Rightarrow$  lower  $\lambda$ .



# Cross-country parameter estimates: Rel. disutility of domestic work $D_c^f/D_c^m$

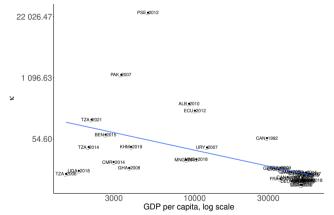
### Gender gap of disutility of care work $D_{c}^{f}/D_{c}^{m}$



Greater gap for  $\frac{L_d^f}{L_d^m}$   $\Rightarrow$  higher  $\delta$ .

### Cross-country parameter estimates: Rel. disutility of market work $\kappa$

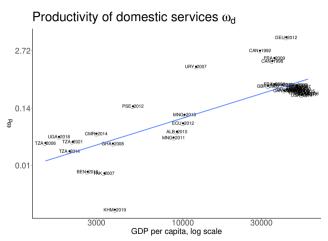
### Gender gap of disutility of market work $\boldsymbol{\kappa}$



Greater  $\kappa$  in LICs needed to explain market work patterns (given wages and care work).

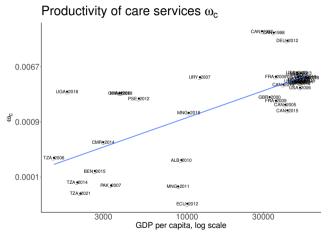


# Cross-country parameter estimates: Valuation/productivity of domestic services $\omega_d$



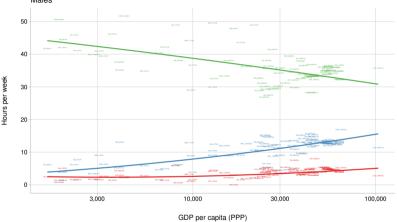
Greater valuation/productivity of domestic services required to explain higher home hours in HICs, despite higher wages.

# Cross-country parameter estimates: Valuation/productivity of care services $\omega_c$



Greater valuation/productivity of care services required to explain higher home hours in HICs, despite higher wages.

## Weekly hours spent on market, domestic and care work per capita Males

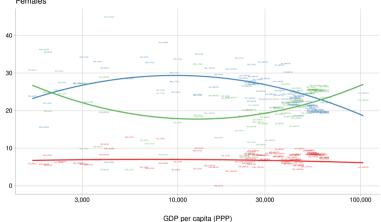


Hours on: - domestic care - domestic services - market work

Quadratic fit, shaded area marks the 95% confidence interval Male working age population. Activity groups are aggregated based on the ICATUS 2016 one-digit codes [market = 182, services = 3, care = 485]. Minimum sample size for each activity group is 30.



## Weekly hours spent on market, domestic and care work per capita Females



Hours per week

Hours on: - domestic care - domestic services - market work

Quadratic fit, shaded area marks the 85% contidence interval
Female working age population, Activity groups are aggregated based on the ICATUS 2016 one—don't codes [market = 18.2, services = 3, care = 48.5]. Minimum sample size for each activity group is 30.



### Appendix model: : Consumption allocation

Ratio of consumption FOCs across genders:

$$\frac{\lambda}{1-\lambda} \left(\frac{c^m}{c^f}\right)^{\frac{1-\sigma\varepsilon}{\varepsilon}} \left(\frac{c_m^m}{c_m^f}\right)^{-\frac{1}{\varepsilon}} = 1$$

$$\frac{\lambda}{1-\lambda} \left(\frac{c^m}{c^f}\right)^{\frac{1-\sigma\varepsilon}{\varepsilon}} \left(\frac{c_i^m}{c_i^f}\right)^{-\frac{1}{\varepsilon}} = 1$$

This implies that

$$\frac{c_m^m}{c_m^f} = \frac{c_i^m}{c_i^f}.$$

Married individuals consume the same share of each good. Let  $\Lambda \equiv c_m^m/c_m$ , such that:  $c_c^m = \Lambda c_c$  and  $c_d^m = \Lambda c_d$ .

▶ Back

### Appendix model: First order conditions

Consumption:

$$c_m^g: \lambda^g c^g \frac{1-\sigma\varepsilon}{\varepsilon} c_m^g - \frac{1}{\varepsilon} = \mu_m P$$
  
 $c_i^g: B_i \lambda^g c^g \frac{1-\sigma\varepsilon}{\varepsilon} c_i^g - \frac{1}{\varepsilon} = \mu_i$ 

Hours worked:

$$L_m^g: D_m^g \lambda^g L_m^g^{\frac{1}{\phi}} = w^g \mu_m$$
  
$$L_i^g: D_i^g \lambda^g L_i^g^{\frac{1}{\phi}} = z_i \mu_i$$

where 
$$g = \{m, f\}$$
,  $\lambda^m = \lambda$ ,  $\lambda^f = 1 - \lambda$  and  $i = \{c, d\}$ 

Step 1: Assume common disutility of care work  $(D_c^f = D_c^m)$ 

$$\frac{L_c^f}{L_c^m} = \left(\frac{D_c^m}{D_c^f} \frac{\lambda}{1 - \lambda}\right)^{\phi} \quad \rightarrow \quad \lambda = \frac{\left(\frac{L_c^f}{L_c^m}\right)^{1/\phi}}{1 + \left(\frac{L_c^f}{L_c^m}\right)^{1/\phi}}$$

 $\rightarrow$  Gender ratio of  $L_c$  reveals utility weights  $\lambda$ .

→ Back

### Step 2:

$$\frac{L_d^f}{L_d^m} = \left(\frac{D_d^m}{D_d^f} \frac{\lambda}{1 - \lambda}\right)^{\phi} \quad \rightarrow \quad \frac{D_d^m}{D_d^f} = \left(\frac{L_c^m}{L_c^f} \frac{L_d^f}{L_d^m}\right)^{\frac{1}{\phi}} \equiv \frac{1}{\delta}$$

- $\rightarrow$  Ratio of  $L_d$  reveals gender gap of disutility of domestic work  $\delta$ .
- → Member who does less domestic relative to care work has a higher disutility.

→ Back

Step 3: Use FOCs for market work to get relative disutilities from market work:

$$\kappa \equiv \frac{D_m^f}{D_m^m} = \left(\frac{L_c^f}{L_c^m} \frac{L_m^m}{L_c^f}\right)^{\frac{1}{\phi}} \frac{w^f}{w^m}.$$

ightarrow Gender wage gap pins down the gender gap of disutility of market work.



Step 4: Assume 
$$D_c^m = C^m$$
 and  $\frac{D_d^f + D_d^m}{2} = C^m$ 

$$\omega_{c} = \left(\frac{L_{m}^{m}}{L_{c}^{m}}\right)^{-\frac{1}{\phi}} \left(\frac{L_{m}^{f}}{L_{c}^{f}}\right)^{-\frac{1}{\varepsilon}} \left(\frac{1}{P} \frac{w^{m} \Delta_{m} + w^{f}}{\Delta_{c} + 1}\right)^{-\frac{1}{\varepsilon}} \frac{w^{m}}{P}$$

$$\omega_{d} = \left(\frac{L_{m}^{m}}{L_{d}^{m}}\right)^{-\frac{1}{\phi}} \left(\frac{L_{m}^{f}}{L_{d}^{f}}\right)^{-\frac{1}{\varepsilon}} \frac{2}{1 + \delta} \left(\frac{1}{P} \frac{w^{m} \Delta_{m} + w^{f}}{\Delta_{d} + 1}\right)^{-\frac{1}{\varepsilon}} \frac{w^{m}}{P}$$

where  $\Delta_m, \Delta_d, \Delta_c$  are gender ratios of work time, and  $\frac{D_m^m}{C^m} = \frac{2}{1+\delta}$ 

Step 5: Level equation for market hours reveals  $C^m$ :

$$C^{m} = L_{m}^{m-\frac{1}{\phi}} (\Lambda \Omega(\omega_{d}, \omega_{c}) L_{c}^{f})^{\frac{1-\sigma\varepsilon}{\varepsilon}} \left( \Lambda L_{m}^{f} \frac{(w^{m} \Delta_{m} + w^{f})}{P} \right)^{-\frac{1}{\varepsilon}} \frac{w^{m}}{P}$$

